



Universiteit  
Leiden  
The Netherlands

# Population-Scale Networks in Official Statistics Use Cases and Privacy Implications

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# Network Science



# Network Science

The study of phenomena emerging from relations between entities.

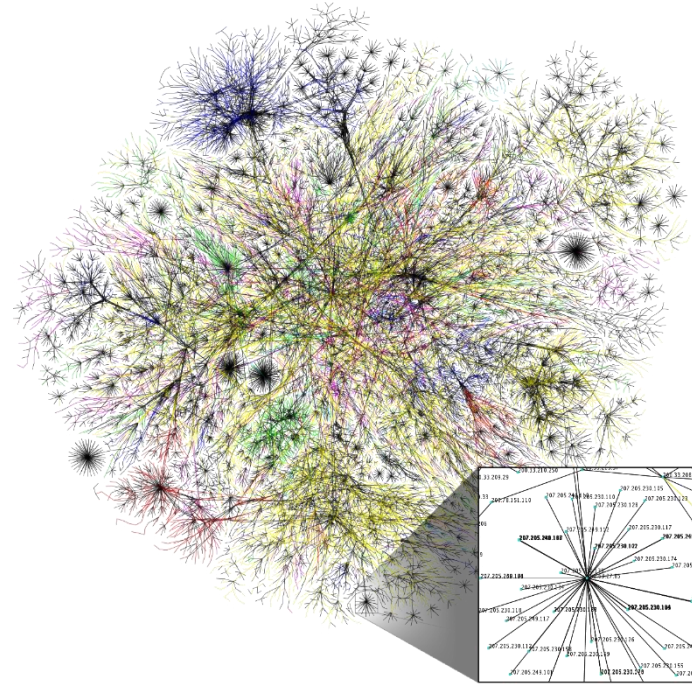
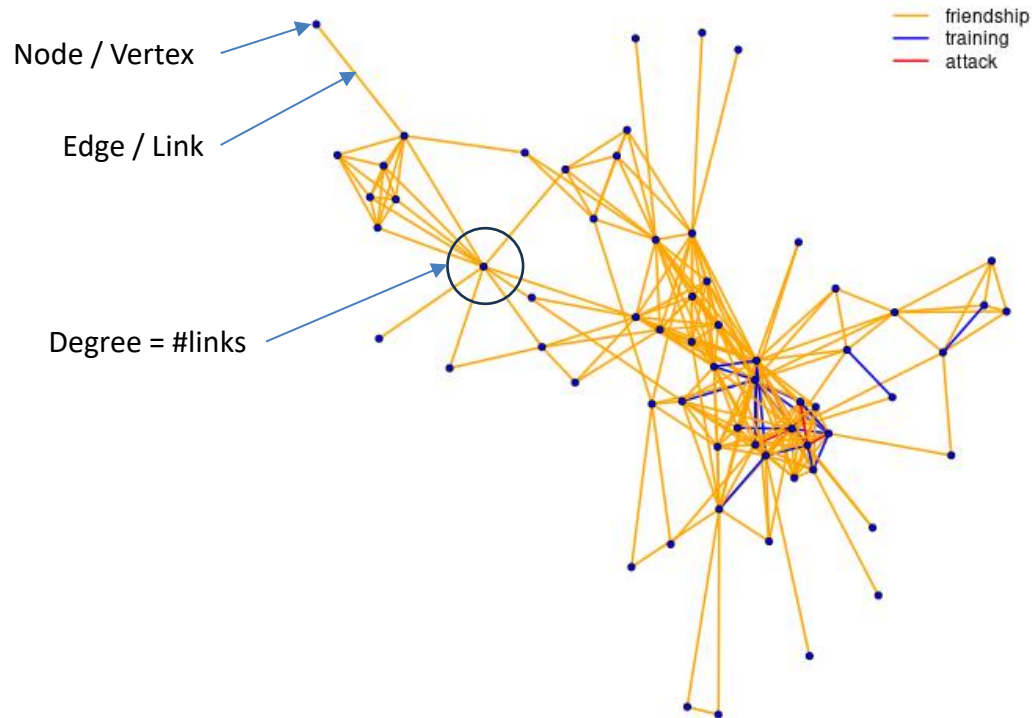


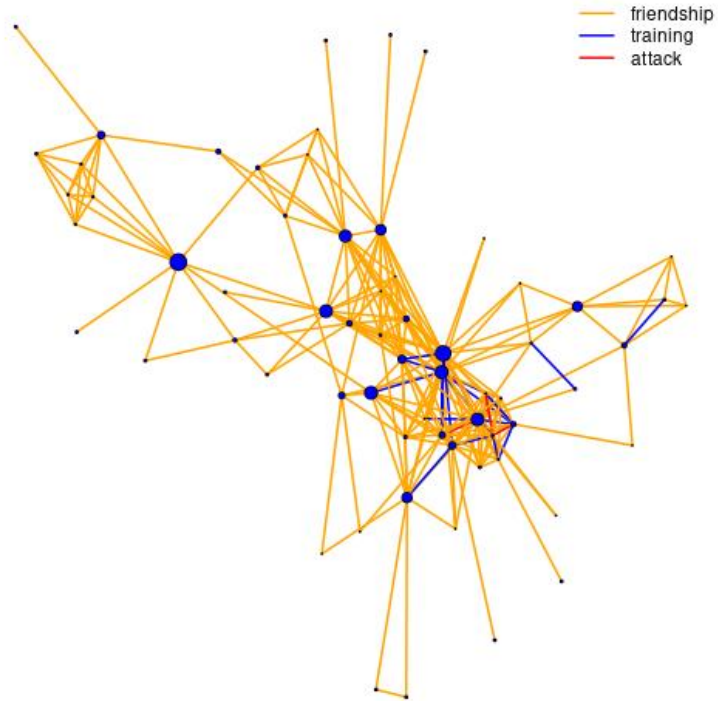
Image: <https://en.wikipedia.org/wiki/Internet>



# Example: the Moreno Terrorist Network



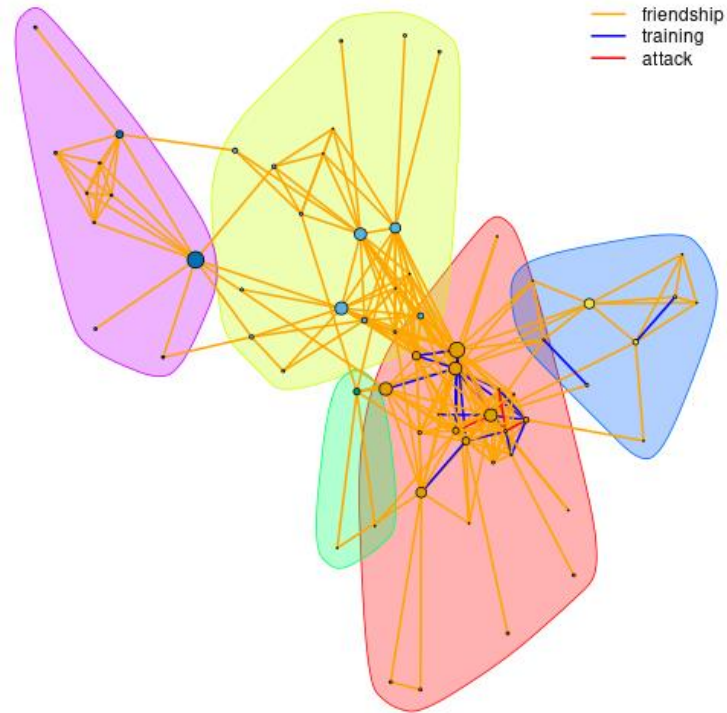
# Importance of nodes: centrality



Betweenness centrality



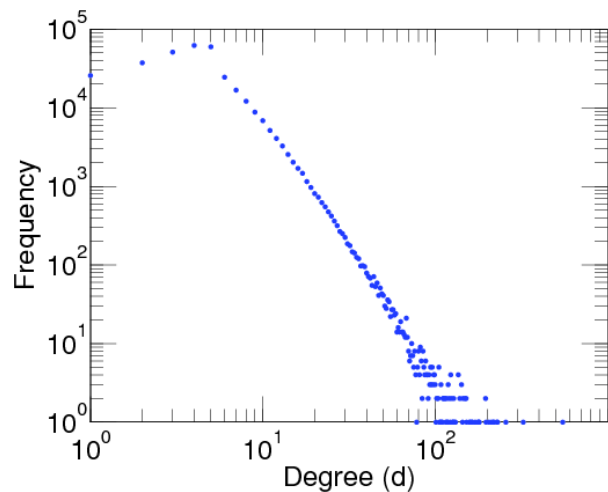
# Clustering of nodes



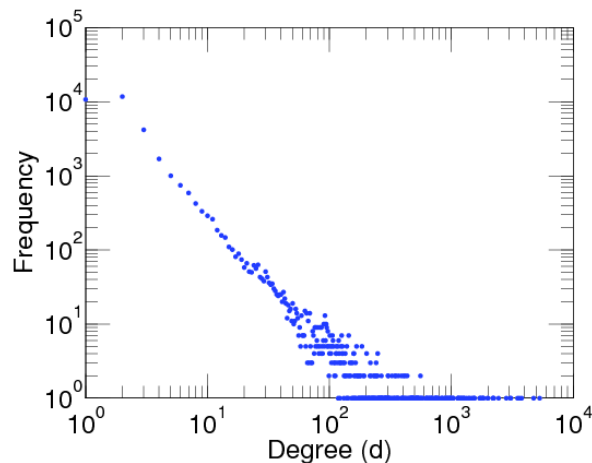
Louvain Clustering



# Network models and universal behaviour



Amazon product co-buying



Internet server connections

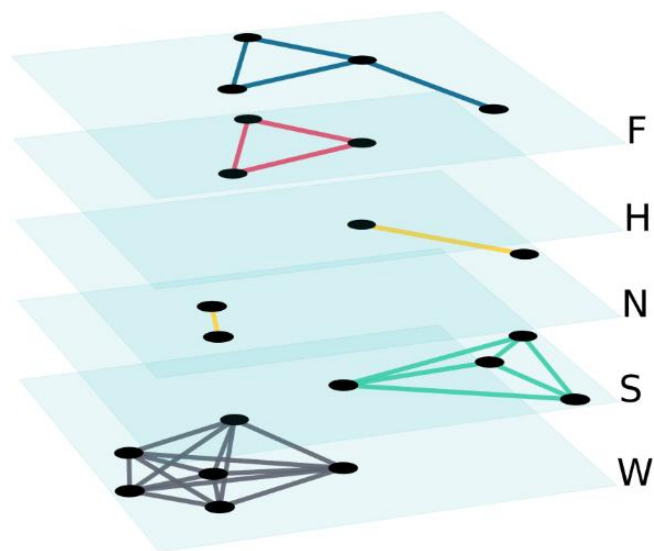


# Population Scale Social Network





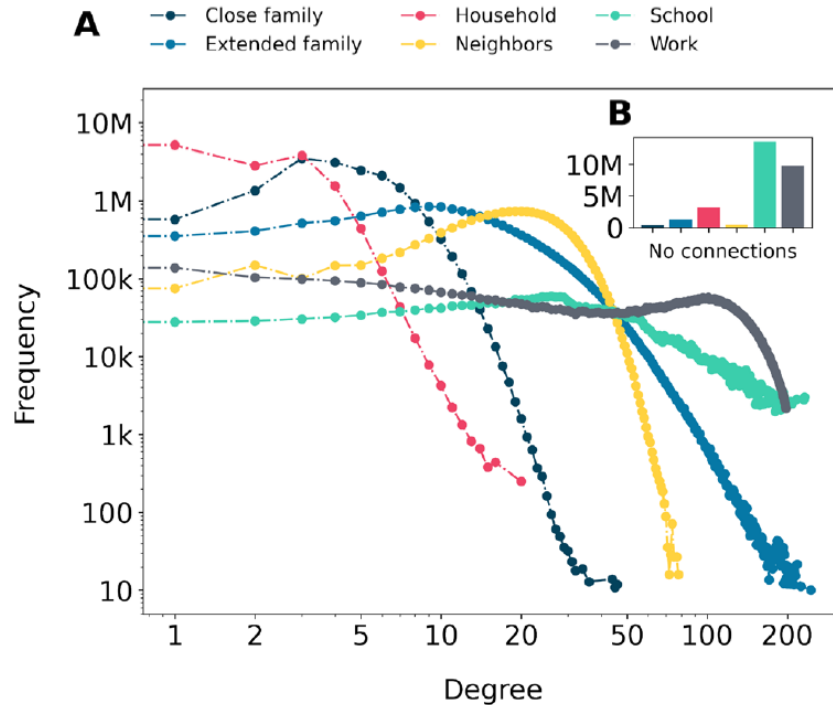
# A Population-Scale Social Network Based on Administrative Data



**F**amily  
**H**ousehold  
**N**eighbours  
**S**chool  
**W**ork



# Some properties



17 Mn nodes

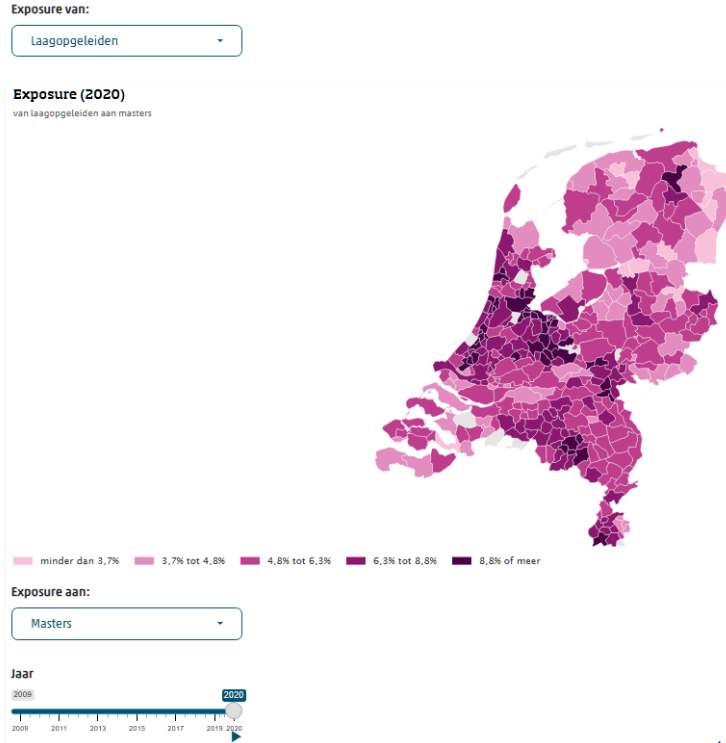
1.4 Bn links

Network as *contact opportunity structure* (social capital)



# Educational Segregation

**Exposure of educational level A to B:**  
Percentage of B in the network  
surroundings of A

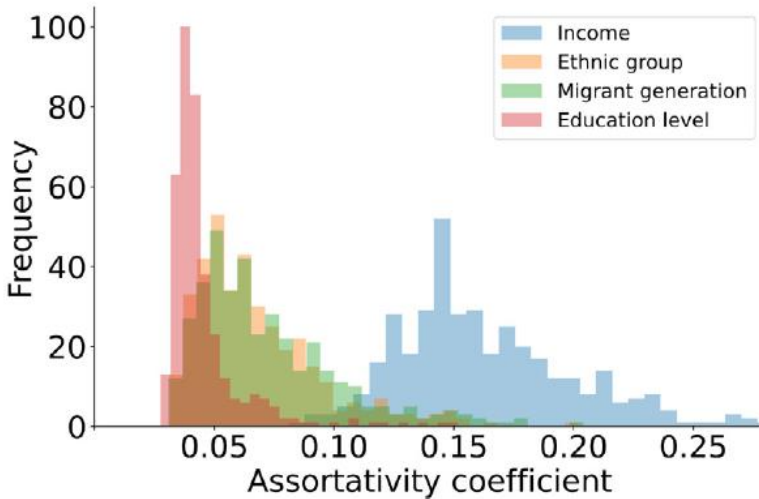


[https://dashboards.cbs.nl/v4/opl\\_segregatie/](https://dashboards.cbs.nl/v4/opl_segregatie/)

Van der Laan *et al* (2023) European Sociological Review **39** 147-160 <https://doi.org/10.1093/esr/jcac026>

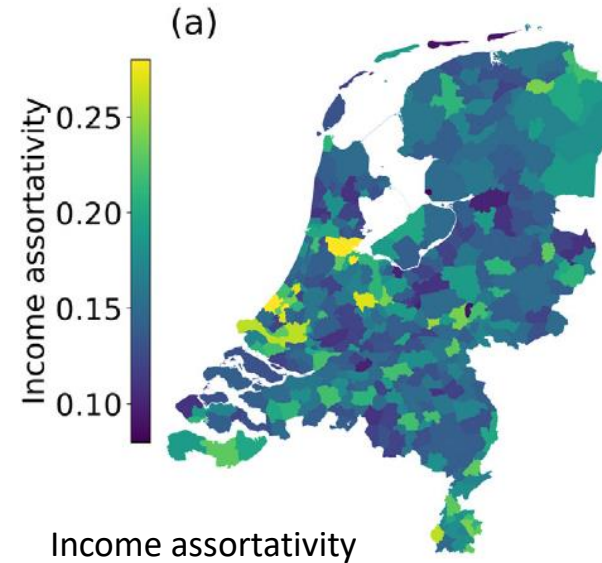


# Socio-economic segregation

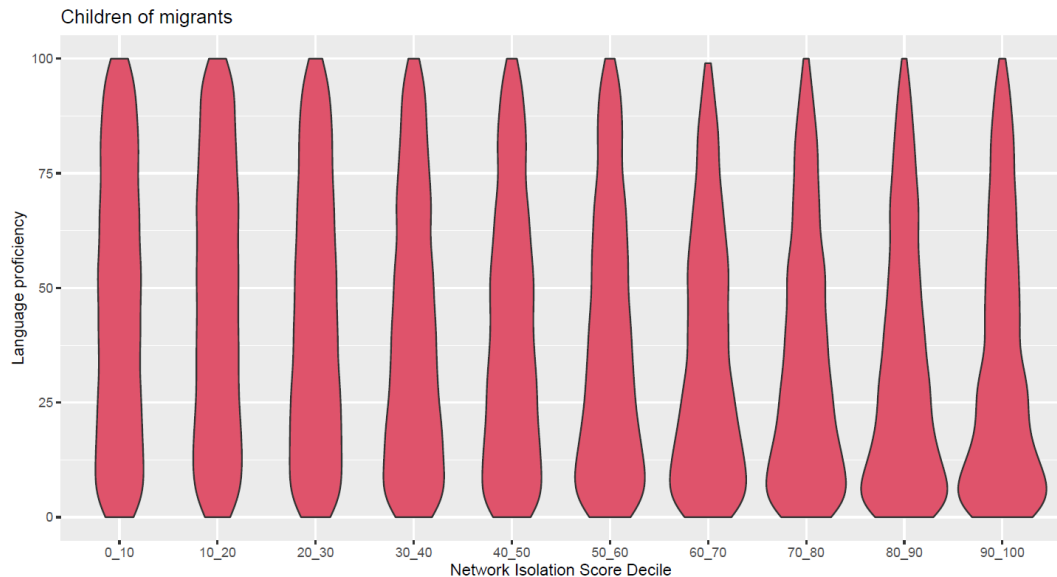


## Assortativity:

The tendency of similar nodes to be interlinked.



# Dutch Language Skills of Migrant's Children



**Network Isolation:** weighted fraction of persons with same migration background in network surroundings of child.

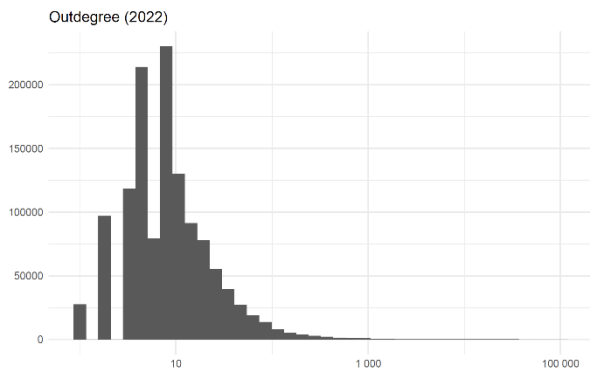
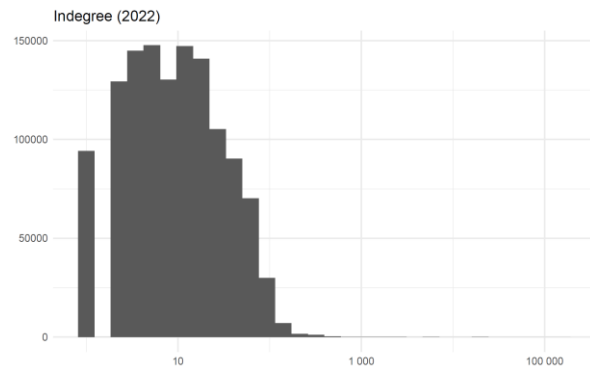
Language proficiency distribution vs Network Isolation



# Population Scale Business Network



# The Dutch Production Network



**Estimation of trading network**

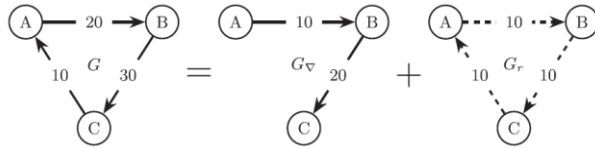
$10^6$  Businesses

$1.6 \cdot 10^7$  Transactions

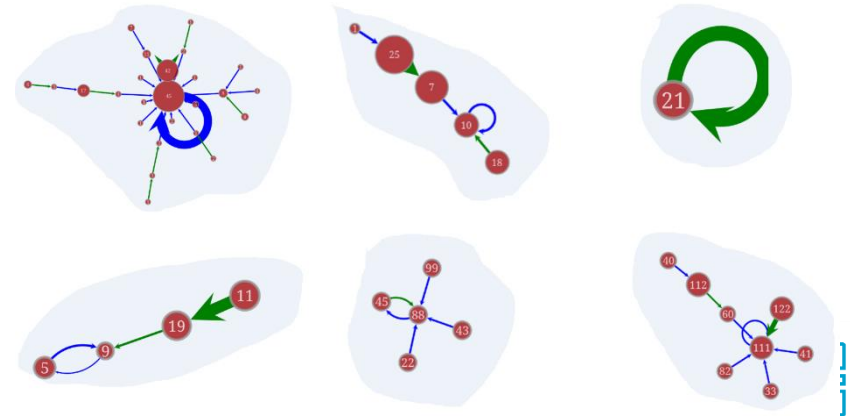
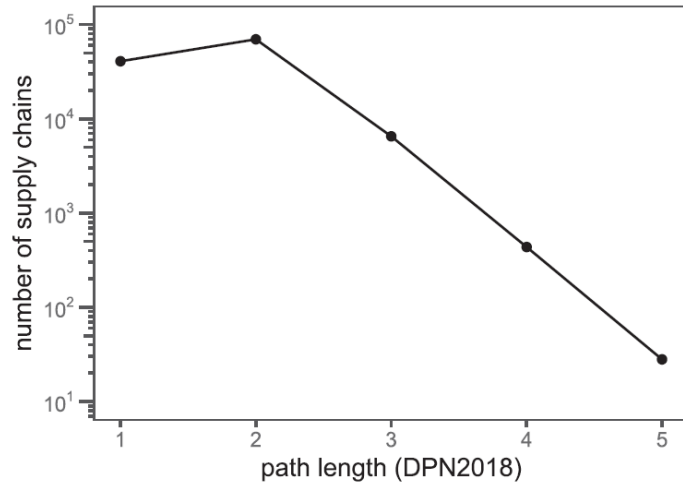
523 Commodity groups

*Links are estimated*

# Detection of Production Chains



**Restricted Gradient Graph Algorithm**  
Splits a graph into cycles and paths.

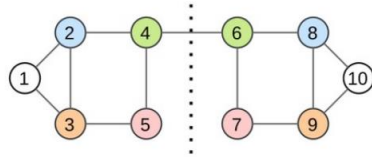




# Privacy and Anonymity in Social Networks



# Anonymity in Complex Networks



## ANO-NET



POPNET



Rachel de Jong <sup>(1,2)</sup>



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*(1) Computational Network Science Group at the Leiden Institute of Advanced Computer Science*

*(2) Statistics Netherlands*



# Research questions

(1) How does **network structure** affect risk of disclosure?

- **Identity**
- Attributes

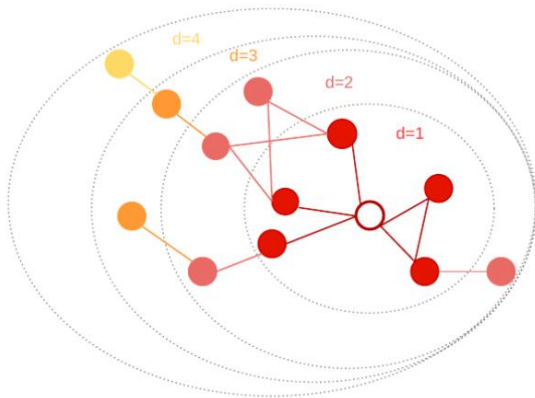
(2) How can we mitigate disclosure risks?

- Utility

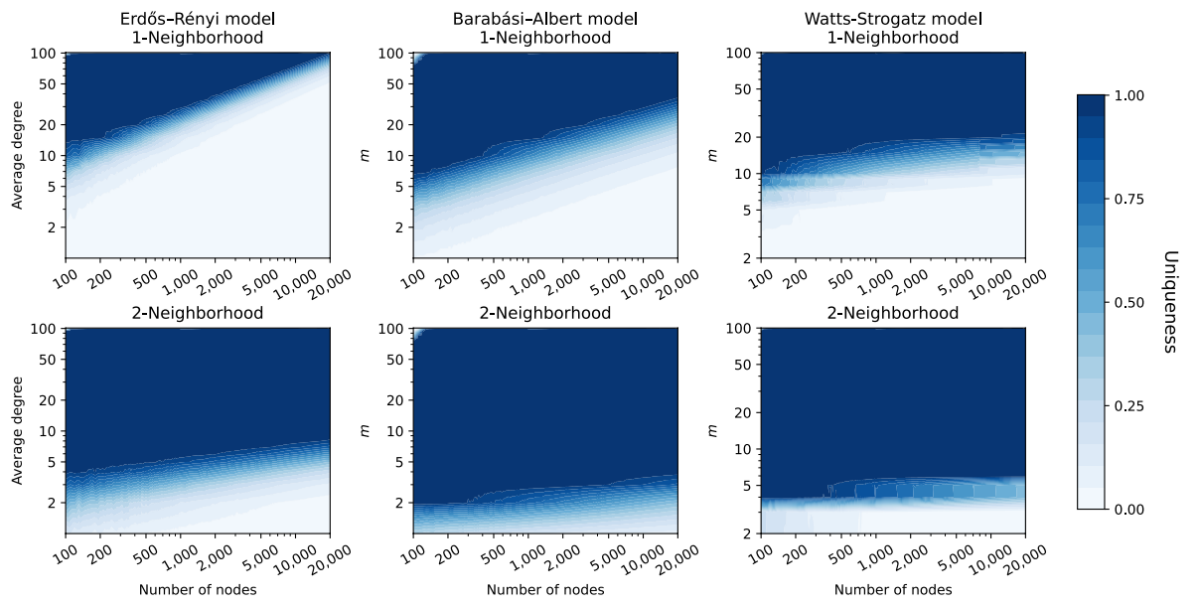


# Graded $k$ -anonymity: $d$ - $k$ anonymity

- Attacker knows *full* network structure surrounding a node, up to and including distance  $d$
- A node is  $k$ -anonymous if there are  $k-1$  nodes with the same neighbourhood.



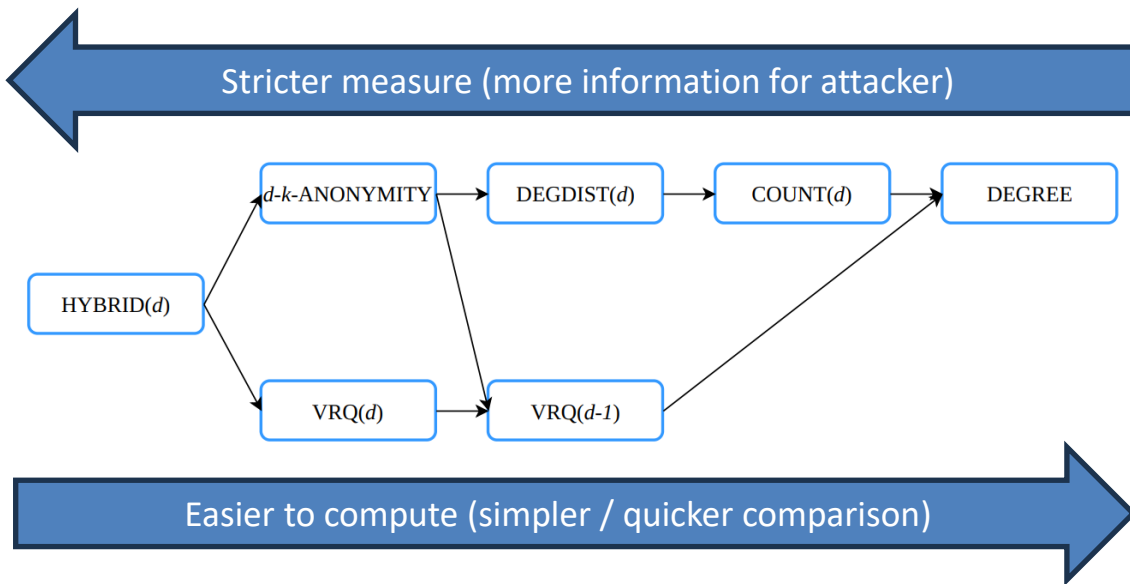
# $d$ - $k$ anonymity



**Most nodes reidentified:**  
If surrounding structure  
upto  $d \leq 2$  is known  
exactly



# Approximating $d$ - $k$ anonymity



**A  $\rightarrow$  B: A is stricter than B**  
Stricter means that the attacker is assumed to have more knowledge.

**Incomplete information over larger distance poses more risk than complete information close by.**

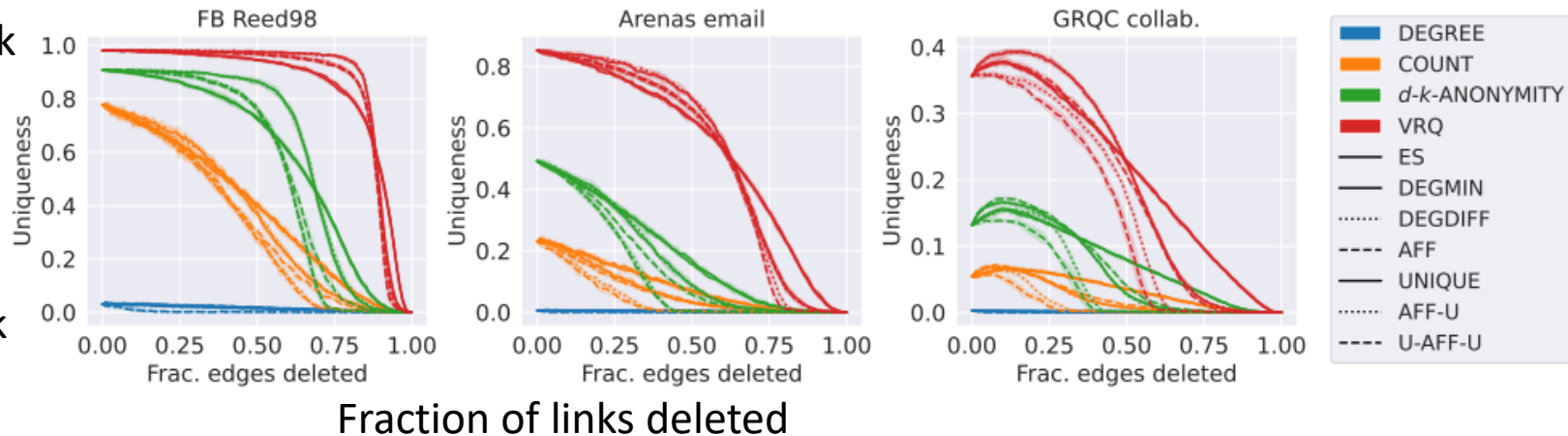
**COUNT( $d$ )** is a good approximation for  $d$ - $k$  anonymity and faster at  $d=1$



# Experimenting with anonymization

High risk

Low risk



- Link deletion is **better** than adding or swapping
- Targeted deletion works ***much better*** than random deletion



# Take-home messages



**Network data** is highly interesting for Statistical Institutes, which often have unique data to construct them.

There already are interesting use cases, **but we are just scratching the surface!**

We are working on **measuring and mitigating disclosure risk** when sharing network data



# Thank you!



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